

Fluctuators in disordered metallic point contacts: a simulation approach

V.I. Kozub* and C. Oligschleger**

*Institut für Festkörperforschung, Forschungszentrum Jülich,
D-52425 Jülich, Germany*

(February 1, 2008)

Electron transport through amorphous monatomic metallic structures generated earlier by molecular dynamics simulations is studied numerically. The interference of electronic trajectories backscattered by the structural disorder probes the multistable structural relaxations responsible for low-frequency noise in real metallic contacts. The structure of these modes is visualized; the dependence of noise magnitude on size and structure of the modes is studied. The transition from multistable behaviour to a more complex one is observed for temperatures far below the melting temperature. The current fluctuations observed numerically resemble the complex behaviour reported earlier for current noise in small metallic structures at moderate temperatures.

PACS 72.10-d, 72.70+m

I. INTRODUCTION

In recent years substantial progress in the study of the flicker noise problem was achieved. This is mainly connected with experiments on small conducting systems, where the $1/f$ noise was decomposed^{1,2} into a sum of contributions due to “elementary” defects with internal degrees of freedom - “fluctuators”. These defects switch between two possible configurations and cause the “telegraph” resistance noise in small contacts. In metallic systems they are believed to be related to structural defects which at low temperatures are seen as the well-known two-level systems³⁻⁸. We would also like to mention works where the two-level fluctuation studied exists in atomic size contacts produced with help of the break-junction method⁹. However, there is still no clear understanding of the microscopic nature of these defects.

Many experimental results can be explained¹⁰ by the model of independent fluctuators described by rate equations for the occupation numbers. The soft-potential approach which relates the fluctuators to some “soft” double-well effective potentials, has been used to describe this picture^{8,10}. It fails, however, to give a microscopic insight into the problem. On the other hand, some experiments revealed a much more complex behaviour exhibiting in particular fluctuator interactions and non-stationary chaotic behaviour of the fluctuator parameters². These features can not easily be described within the framework of the soft-potential model. Thus a microscopic analysis of the problem would be desirable. However, a description of disordered materials based on purely analytical methods meets obvious difficulties. Numerical simulations based on molecular dynamics (MD) methods are used successfully to model the structure of glassy materials as well as their thermodynamic properties including the density of states. In particular, many details related to low-energy vibrational excitations in these materials have been revealed this way¹¹. To our knowledge, electron transport through disordered media has not been treated by these numerical methods. Real metallic point contacts studied experimentally can

be as small as 3 – 10 nm in diameter and thus consist of only $\sim 10^3 - 10^4$ atoms which is just of the order accessible to numerical simulations. Moreover, the structure of these constrictions is not expected to be perfectly crystalline especially in view of the amorphous films used to prepare these point contacts.

Therefore, it is attractive to use a simulation approach to study slowly relaxing metastable configurations in disordered metallic structures with an application to low-frequency noise. In the following we will give the results of a first such study of noise within the framework of simplified model considerations.

The main results of our paper described in the following are: 1) We have identified local atomic arrangements leading to metastable configurations. 2) A transition from a simple telegraph signal to a more complex behaviour with increasing temperature was observed which reproduces the experimental behaviour; it is important that the ratio of this “critical” temperature to the melting temperature agrees with experiment. 3) The magnitude of the resistance fluctuations and its dependence on the number of atoms forming the “fluctuator” is considered; the results of the simulations are in agreement with experiment.

II. THEORETICAL ASPECTS

Our aim is to analyze numerically charge transport through disordered structures prepared previously by molecular dynamics¹². The structures studied are considered to model a 3D cubic microbridges (with side-length a) between bulk contacts. The atoms forming the structures are taken to be scatterers for the incident electrons. We consider the weak scattering limit where the mean free path of the electrons, l , is larger than a . This implies that the scattering cross-section s obeys the inequality $n_i s < a^{-1}$ where $n_i = N/a^3$ and N is the total number of atoms in the structure. In real glassy metals the mean free path is significantly larger than the electron wavelengths, and therefore, the approximation is justified for

nanoscale point contacts.

To study the conductance changes caused by “jumps” in the structural configurations we relate them to the changes of the interference contribution to the backscattered electron flux in the contact region. The weak scattering approximation allows us to neglect multiple scattering, restricting our calculations to a minimal number of scattering events. This corresponds to the concept of local interference which has been introduced in Ref. 13 for the case of scattering by complex defects¹⁴. Mesoscopic effects in bulk samples caused by local interference of a more general type have been considered in Ref. 15.

The standard approach to the conductance G of small contacts exploits the Landauer formula (see e.g. Ref. 16)

$$G = \frac{e^2}{h} \sum_{\alpha} (1 - R_{\alpha}) \quad (1)$$

where R_{α} is the reflection coefficient for channel (mode) α . In a simulation one needs to identify these modes α . This can easily be done for 2D quantum point contacts with smooth “adiabatic” boundaries¹⁷ whereas for realistic structures one meets with considerable problems. In particular we mention Ref. 18 where for the case of a short 2D channel the conductance is calculated numerically by matching the “bulk” plane wave modes to the channel’s transversal modes.

Here, we will apply the “wave optics” approach which was developed for the transport in structures with a small number of scattering events and is in the spirit of Ref. 18. In Ref. 19 this approach was developed and successfully applied to analyze experimental data on mesoscopic transport in 3D ballistic point contacts with diffusive surroundings. We also want to mention the simulations of quasi-ballistic transport in static disordered structures²⁰ based on the Green’s function method whose results agree well with those of Ref. 19.

The “wave optics” approach exploits the fact that for metallic point contacts transport is always semiclassical in the sense that the number of quantum channels is large, corresponding to the “geometrical optics” approximation for the de Broglie waves. For an ideal point contact, separating the bulk leads, the modes α correspond to the “optical beams” cut by the orifice from the incident plane waves \mathbf{k} . The “quantization” of the modes originates from the Fourier expansion of the kernel of the Fresnel–Kirchhoff integral which describes the diffraction of the incident plane wave by the aperture in an opaque screen, see e.g. Ref. 21. The number of the modes, $\sim (k_F a)^2$ (with \mathbf{k}_F the Fermi wave vector), is the number of independent solutions of the diffraction problem for a given $|\mathbf{k}| \approx \mathbf{k}_F$.

To calculate the backscattering coefficients R_{α} within this approach we use the standard perturbation theory of scattering with Schrödinger’s equation²². We consider the scattering of the incoming modes ψ_{α} which, as discussed above, at distances of the order of the atomic scale can be approximated by plane waves with wave vectors

\mathbf{k}_{α} . The resulting wave, scattered by a scatterer i at point \mathbf{R}_i , is

$$\psi_{s,\alpha}(i, \mathbf{r}) = \frac{\psi_{\alpha}(\mathbf{R}_i) F_i}{|\mathbf{r} - \mathbf{R}_i|} \cdot \exp(ik |\mathbf{r} - \mathbf{R}_i|). \quad (2)$$

Here F_i is the scattering amplitude which in the following we assume to be equal for all scatterers ($F = (s/4\pi)^{1/2}$). Including multiple scattering would add higher order terms in F/a . For a random distribution of scatterers the sum over all possible configurations would give a factor $\sim N^{1/2}$ to the correction of the wave function Eq. 2. Thus the total contribution of trajectories involving multiple scattering is by a factor $s^{1/2} N^{1/2} / (a(4\pi)^{1/2}) = s^{1/2} n_i^{1/2} a^{1/2} / (4\pi)^{1/2} \ll 1$ smaller than the contribution due to single scattering, i.e. neglecting multiple scattering is justified.

The coefficient R_{α} is by definition the ratio of the “backscattered” current to the “incident” current of the mode α . In our approximation we have:

$$R_{\alpha} = \frac{1}{v_{\perp,\alpha} |\psi_{\alpha}|^2} \int_S d^2\mathbf{r} \frac{ie\hbar}{2m} (\langle \psi_{s,\alpha}^* | \nabla | \psi_{s,\alpha} \rangle + c.c.). \quad (3)$$

Here $\psi_{s,\alpha}$ is the sum of the waves scattered by the scatterers i , $v_{\perp,\alpha}$ is the velocity of the incident electron wave perpendicular to the aperture. The apparent divergency due to $v_{\perp,\alpha}$ in Eq. 3 is integrable due to $v_{\perp,\alpha} \propto (k_F - k_{\alpha,\perp})^{1/2}$, with $\mathbf{k}_{\alpha,\perp}$ the projection of \mathbf{k}_{α} onto the orifice plane, and does not affect the final result of Eq. 4. S is the orifice area while \mathbf{r} is the 2D radius-vector in the detector plane. Fig. 1 depicts schematically two backscattered trajectories which interfere in the detector plane.

From Eqs. 2 and 3 we get for the change of the conductance due to backscattering:

$$W_b \equiv \frac{\delta G_b}{G} = \frac{F^2}{\sum_{\alpha} (1 - R_{\alpha})} \cdot \sum_{\alpha} \int_S d^2\mathbf{r} \cdot \frac{\sum_{i,j} \cos(k_F(|\mathbf{r} - \mathbf{R}_i| - |\mathbf{r} - \mathbf{R}_j|) + \mathbf{k}_{\alpha}(\mathbf{R}_i - \mathbf{R}_j))}{|\mathbf{r} - \mathbf{R}_i| |\mathbf{r} - \mathbf{R}_j|} \cdot (\cos(\angle(OX, \mathbf{r} - \mathbf{R}_i)) + \cos(\angle(OX, \mathbf{r} - \mathbf{R}_j))) \quad (4)$$

Here OX is the contact axis. Eq. 4 is the basic input for the numerical studies described below. The advantage of the coordinate representation used in our approach is its direct contact to the simulation of electron transport through the structure. In our calculations we consider amorphous structures where all atoms act as scatterers. For relatively clean crystalline structures only defect atoms are responsible for backscattering. We are mainly interested in the changes of the backscattering due to changes of the structures and use all atomic positions as input for Eq. 4. In the absence of defects one would obtain the conductance of purely ballistic contact from the Landauer formula of Eq. 1.

III. COMPUTATIONAL DETAILS AND RESULTS

With the help of Eq. 4 we carried out numerical studies of the backscattered current for amorphous and crystalline monatomic metallic structures and for amorphous selenium. We would like to note, however, that dealing with monatomic metallic glasses one meets difficulties due to their strong tendency to crystallize. This problem is known both from experiments on real metallic glasses and from computer simulations. One consequence is that the structural relaxations are mostly irreversible, preventing the formation of multistable structures supposed to give rise to the “fluctuators”. We will discuss these problems in more detail in relation to the results of our simulations. Additionally we have calculated the backscattered electron flux by using a more complex structure of amorphous Se, which is much more stable against crystallisation. The results of the MD-simulation^{23,24} have shown that both soft sphere and Se glasses behave similarly with respect to their dynamics which in both systems at low temperature exhibits local relaxations. Although electron transport in real Se-based structures is hardly similar to that in metals, we believe that the simulations for the corresponding model structures are in any case instructive. Indeed, one should keep in mind that “fluctuators” are thought to be related to defect regions where the structure might be even more complex than in a monatomic metallic glass.

The metallic structures were generated in earlier MD-simulations^{11,12,24}. The interatomic interaction in these systems is given by a soft sphere potential $V(r) = \epsilon(\sigma/r)^6 + A(r/\sigma)^4 + B$ where the energy-scale is given in units of ϵ and the length-scale in units of σ . In the simulations we used the units $\epsilon = \sigma = m = 1$, m being the atomic mass. The density is kept constant at $\rho\sigma^3 = 1$ and the nearest neighbour distance corresponds to about 1.1σ . To reduce the numerical effort the potential is cut off at $r_c/\sigma = 3.0$ and shifted by a polynomial $A(r/\sigma)^4 + B$ with $A = 2.54 \cdot 10^{-5}\epsilon$ and $B = -3.43 \cdot 10^{-3}\epsilon$. Both the potential and the force are zero at the cut-off. Such a potential is appropriate to model metallic systems²⁵.

As described by Laird and Schober¹¹ to bypass crystallization the model glassy structures were produced from well equilibrated liquids by a rapid quench. With typical quench-rates of the order $0.25k_B/\sqrt{m\sigma^2}/\epsilon$ the configurations are cooled to roughly half the glass temperature T_g and left there for more than 1200 molecular dynamics time-steps (MDS), i.e. about 60 typical vibration periods, to stabilize the potential energy. The local minima of the structures were found by minimizing the potential energy with a steepest descent/ conjugate gradient algorithm²⁶. To have a reasonable statistics for the structures consisting of 500 and 1024 atoms in all 60 and 21 model glassy structures were produced, respectively.

The structural changes of these metallic glasses were observed in a previous molecular-dynamics simulation¹². To study the dynamics of these soft sphere glasses they

were heated with help of the “Velocity-Verlet”-algorithm in stages to temperatures ranging from 0.05 to $0.125 T_g$. The molecular dynamics was done with periodic boundary conditions to reduce surface effects. After heating the glasses to the desired temperature, the temperature was kept constant by scaling the velocities of the atoms. At each temperature the dynamics of the systems was followed for 9000 time-steps, which corresponds roughly to 500 periods of a typical vibration.

To observe more complex structures and to reduce further the “finite size” effects additionally 15 soft-sphere-glasses with $N = 5488$ were generated from hot melts and used to study relaxations in a greater detail²⁴. These glasses were heated to temperatures ranging from 0.05 up to $0.15 T_g$ and left there for 90000 MDS (an order of magnitude longer than the smaller systems).

During the molecular dynamics simulations at constant temperature the configurations move to new minima of the energy landscape due to local hopping processes over small energy-barriers. To detect new configurations on the energy hypersurface the displacements of the atoms from the metastable equilibrium positions \mathbf{R}_n^i of atom n in configuration i are measured and the total displacement of the structure is defined as:

$$\Delta R^2(t) = \sum_n (\mathbf{R}_n(t) - \mathbf{R}_n^i)^2 \quad (5)$$

where $\mathbf{R}_n(t)$ is the actual position vector of atom n . If the total displacement of the atoms exceeds a cut-off value and the residence time of the atoms in the new positions also exceeds a minimal period of at least three soft, low-frequency vibrations (several 100 MDS) the new positions of the particles are accepted as a new minimum configuration. The cut-offs of displacement and resident time, respectively, are chosen such that spurious minima are avoided. This procedure is described in greater detail in Ref. 12,24.

These minima are monitored during the molecular dynamics runs. The corresponding relaxations from one minimum to another can be either reversible or irreversible. The irreversible jumps are mainly due to the instability of the monatomic metallic glasses. This instability manifests itself in the fact that during the observation time some of the samples partially crystallized. Such a crystallisation is connected with a global rearrangement of nearly all atoms in the configuration. This effect depends strongly on the size of the samples used in the simulation. The larger the system, the more stable are the configurations. The largest systems show greater stability towards crystallization; just one configuration (out of 15 with $N = 5488$ atoms) crystallized during the observation time at a temperature $T = 0.15T_g$. But the tendency to lower the potential energy prevails during the simulation.

Therefore, the first jumps after heating up to different temperatures are related to non-local rearrangements of the glasses, i.e. jumps with large displacements involving

many atoms and leading to more stable configurations. These jumps are followed by relaxations located on only a few atoms. A measure for the localization of a jump is the effective mass

$$M_{\text{eff}} = m \cdot \frac{(\Delta R)^2}{|\Delta \mathbf{R}_{\text{max}}^2|} \quad (6)$$

where $(\Delta R)^2 = \sum_n (\mathbf{R}_n^i - \mathbf{R}_n^f)^2$ is the square of the total distance ΔR between two successive minimum configurations (called “initial” and “final” positions of the jump). $\mathbf{R}_n^{i,f}$ denotes the respective initial and final positions of atom n , $|\Delta \mathbf{R}_{\text{max}}^2|$ is the maximal distance a single atom jumps in this relaxation. Since we take the masses of the atoms comprising the structures as equal, M_{eff} counts the effective number of particles contributing to the hopping process.

In an extended computer simulation it is found that the displacement of a single atom in the relaxation is only a fraction of the nearest neighbour distance (typically a tenth of a bond length), i.e. relaxations at low temperatures are local processes with small displacements of the atoms contributing to this thermally activated jump. However, even the small displacements of the single activated atoms exceed the vibration amplitudes. Since the typical total distance between two minimum configurations is about one or several nearest neighbour distances²⁷, the effective mass is of the order of 10 to 100 atoms contributing essentially to the relaxations. It is found that these entities of some ten particles involved in the hopping processes form chain-like structures which move collectively along these chains²⁸.

Since we are interested in multistable configurations, we restrict ourselves to the relatively rare reversible changes of the configurations, which means that the initial configuration and the final one of successive jumps are identical. A measure for the reversibility of successive jumps can be given by the quantity $c_{RR'}$

$$c_{RR'} = \frac{1}{\Delta R \Delta R'} \sum_{n=1}^N |\Delta \mathbf{R}_n| |\Delta \mathbf{R}'_n| \quad (7)$$

where $\Delta \mathbf{R}_n = (\mathbf{R}_n^i - \mathbf{R}_n^f)$ is the displacement vector of atom n in the relaxation ΔR ($\mathbf{R}_n^{i,f}$ being, as above, the initial and the final positions of atom n in the relaxation ΔR), and ΔR and $\Delta R'$ are the total jump-lengths of two successive relaxations given by $\Delta R^2 = \sum_{n=1}^N (\Delta \mathbf{R}_n^2)$. For a reversible jump one has $c_{RR'} = 1$, i.e. the same atoms are contributing equally to both jumps. If the jumps are uncorrelated, $c_{RR'}$ would be of the order of $c_{RR'} = N_p/N$, where N_p is the number of atoms involved in the hopping. During the MD-runs of the 60 glasses with 500 atoms only two structures undergo reversible jumps, whereas for the glasses with 1024 soft spheres only one reversible relaxation occurred. The effective masses of the reversible relaxations observed in soft-sphere-glasses with $N = 500$ and 1024 atoms range from 6 to 16 atomic masses. At $T \approx 0.1T_g$ half of the glasses with $N = 5488$ settled

during the observation time to configurations where reversible jumps involving up to four local minima are observed. For the simulations with 5488 atoms reversible relaxations with effective masses from 9 to 50 atoms were found.

In order to calculate the electron back-flow we use incident electron waves with \mathbf{k} -vectors of length $k = \pi/\sigma$. This value determines the “discretization” of the numerical integration in Eq. 4. The summation over the modes in Eq. 4 becomes a sum over discrete angles which we take as $\Delta\phi = 2\pi/ka$ and $\Delta\theta = \pi/ka$, where a is the side-length of the amorphous sample, for the metallic glasses the side-length is $a = N^{1/3}\sigma$. Using different grids for the numerical discretization changes the results by a few percent only, i.e. they are not crucially sensitive to the specification of the modes. To escape numerical problems with vanishing denominators in Eq. 4 we integrated over r not in the front orifice plane but instead in a “detector” plane shifted by approximately one atomic distance from the orifice plane. The integration becomes a double-sum with $x = i\Delta x$ and $y = j\Delta y$ where $\Delta x = \Delta y = 1/k$. The detector plane is taken about 2 to 3 times larger than the orifice; the thus neglected backscattered current is less than 10 – 25%. As value of the scattering amplitude F , we take (typical for metals) $k_F F \simeq 1$. One can show that for a relatively small contact volume (small a and N) the weak scattering approximation ($sN/a^2 < 1$) holds with this assumption.

To test our procedure we applied it to the simple case of a self interstitial atom in an fcc metal. This so called dumbbell configuration is formed by replacing one atom by a pair of atoms aligned in (100) direction²⁹. The elementary jump process of this self interstitial atom configuration is to a nearest neighbour site and involves a change of orientation to a different cubic axis, i.e. the dumbbell is now aligned in (010) or (001) direction. Using the soft sphere potential we construct configurations comprising 501 atoms with the dumbbell in the middle of the structure aligned in (100) and (001) directions. The coordinates of the atoms are then used as input for Eq. 4 to calculate the backscattering of these structures. For the configuration with the dumbbell in (100) direction, i.e. perpendicular to the detector plane (see Fig. 1) we find $W_b = 0.536$, and for the two other orientations (001) and equivalently the (010) alignment, parallel to the detector plane, we calculate $W_b = 0.540$. From this we deduce that the relative magnitude of the fluctuation due to the reorientation of the dumbbell is about 0.7%.

In the following we present the relative magnitudes of the fluctuations caused by jumps and relaxations in monatomic metallic glasses and defect structures as described above. Since we are interested in the changes of the backscattered flow due to relaxations of the samples we determine the minima observed in the MD runs and calculate W_b for these structures corresponding to the local minima of the potential energy. We neglect the contribution of atomic vibrations to the electronic backscattering which will be similar for different configurations.

In Fig. 2 we show W_b for a metallic glass with $N = 500$ atoms. After the initial rearrangement connected with a decrease in potential energy, the system was stable for more than 20000 MDS before a reversible jump occurred with a total jump-length of $\Delta R = 1.03\sigma$ and an effective mass $M_{\text{eff}} = 16m$. The relative magnitude of the backscattered current is about 0.6%.

Fig. 3 shows W_b for a system with $N = 1024$ atoms. After approximately 6000 time-steps a reversible jump occurred with a total jump-length of $\Delta R = 0.44\sigma$ and an effective mass $M_{\text{eff}} = 6m$. The fluctuation due to the structural relaxation is approximately 0.2% of the total interference contribution.

To simulate more complex multistable atomic aggregates larger samples are needed. Indeed as we have discussed the smaller systems are relatively unstable thus preventing extended multistable atomic aggregates. Therefore, we have also studied the current transport based on the results for a glass with $N = 5488$ atoms. To shorten simulations of the interference pattern we restricted the summations over the scattering atoms R in Eq. 4 to a subset $N_s \approx 700$ of the atoms including and surrounding the active ones.

The conductance change of this glass heated to $0.1T_g$ and aged for 90000 MDS is shown in Fig. 4. In Fig. 4(a) we show the signal of the backscattering for the detector placed perpendicular to the arbitrarily chosen x-axis of the structure, in Fig. 4(b) we measure the backscattered current in the plane perpendicular to the z-axis of the point contact, i.e. we have placed the detector parallel to the x-y-plane of the sample of the configuration and the bulk leads are now perpendicular to the x-y-plane of the nanoscale point contact. The results of the backscattering are much more complex than the ones described above for the smaller systems: the complex behaviour of the conductance change shown in Fig. 4 results from 15 jumps between eight minima denoted by A,B,C,...,H according to their occurrence during the simulation. After an initial drop in energy the glass relaxes to a (meta)stable region in the configurational space, where we monitored these strongly correlated jumps between 8 minima of nearly equal energy. After about 17000 MDS a reversible jump ($E \rightarrow F \rightarrow E$) occurred with a total jump-length $\Delta R = 0.72\sigma$ and an effective mass $M_{\text{eff}} = 16m$. At $t \approx 42000$ MDS the glass returns to minimum A and relaxes to minimum C ($\Delta R = 1.22\sigma$ and $M_{\text{eff}} = 18m$) and again back to minimum A. After visiting two other minima G and H, the jump pattern ($A \rightarrow C \rightarrow A$) is repeated.

The magnitude of the relative backscattered electron flux is about 0.037% for the contribution of the first reversible relaxation ($E \rightarrow F \rightarrow E$) measured in a detector plane perpendicular to the x-axis of the sample (see the experimental setup in Fig. 1) and 0.032% for the second pronounced fluctuation ($A \rightarrow C \rightarrow A$).

The signal of these fluctuators changes drastically when we measure the backscattered current in the plane perpendicular to the z-axis of the configuration. As de-

scribed above we have placed the detector parallel to the x-y-plane of the sample. The change of the experimental setup enables us to detect inhomogeneities in the structure and in the dynamics of the nanoscale point contact. The first reversible jump ($E \rightarrow F \rightarrow E$) causes a change of the relative magnitude of the backscattered electron flux of approximately 0.11% and the second one ($A \rightarrow C \rightarrow A$) leads to a relative change in the current of about 0.66%. These changes of the signals with respect to the axis may be due to the strong displacements of the atoms in z-direction in both reversible relaxations.

Additionally we calculated the backscattered current also for a partially crystallized defect structure of $N = 500$ atoms. After heating to $0.05T_g$ the configuration begins to crystallize. During the observation time the sample relaxes to another defect configuration. The initial relaxation is accompanied by a large drop in energy ($\Delta E = 30.28\epsilon$) while the following jumps lead to minima with similar energies ($\Delta E < 10^{-7}\epsilon$), in the last relaxation the system jumps to a minimum with slightly higher energy than the one preceding ($\Delta E = 0.00670\epsilon$). The corresponding jump-length is $\Delta R = 13.70\sigma$ for the initial relaxation. For the three following jumps ($\Delta R = 5.23\sigma, 7.75\sigma, 6.83\sigma$) with small energy changes we find effective masses $M_{\text{eff}} = 68m, 74m, 72m$, respectively. For the last jump the effective mass is about $74m$ and the jump-length is about 6.53σ . The jumps following the initial decrease in energy are strongly correlated, i.e. mostly the same atoms are involved. Fig. 5 shows the results for the calculations of the backscattering flow W_b plotted vs. the observation time. The amplitude of the fluctuations after the initial step is about 3%.

So far we have considered monatomic metallic glasses, where due to crystallization effects long observation times are not accessible. Compared to the soft sphere glasses the models for selenium are more stable, and longer observation times are possible without an appreciable drop in potential energy. Therefore, we also report results of the backscattered electron flux, normalized with respects to the incident flow, for a selenium glass. Although selenium is not a metal, the complex structure comprising chains and rings may be a good model for atomic entities forming the “fluctuators”.

The interaction of the Se-atoms is described by a short-range three-body-potential³⁰. The glasses are produced by quenching corresponding liquids with quench-rates of $T = 10^{12} - 10^{14}$ K/s and pressures up to 10 GPa²³. Note that if the quenching would be too rapid density fluctuations of the liquid could be frozen in. One possible way to avoid the formation of resulting micropores is to apply lower quench-rates and/or pressure. The glasses are heated to temperatures of about $0.30T_g$ and then observed for approximately 0.5 ns at every temperature (this corresponds to roughly 3400 high frequency vibrations). In Fig. 6 we plot the backscattered flow W_b versus time for a glass of $N = 750$ atoms at $T \approx 0.04T_g$. One can clearly observe a telegraph signal caused by a reversible jump occurring four times during the observa-

tion period. Its effective mass is $M_{\text{eff}} = 10$ and its total jump-length $\Delta R = 0.5\text{\AA}$. The amplitude of the fluctuation is about 0.42% of the total interference contribution to the backflow.

IV. DISCUSSION AND CONCLUSIONS

We calculate the conductance fluctuations via the standard Landauer formula from the change of backscattering by the atoms comprising the junction. For the small junctions considered here electron scattering can be treated ballistically in the weak scattering limit.

In geometries where multiple scattering is important different methods have to be used. Todorov and Sutton, and Bratkovsky et al. combine a molecular dynamics simulation with a T-matrix approach in tight binding approximation to calculate the conductance through atomic-scale metallic contacts during pulloff^{31–33}. In agreement with experiment they observe conductance jumps due to atomic rearrangements in the tip.

We want to point out that our approach is not suitable to reproduce the limiting case where the point contact merges into the crystalline structure. In this limit the conductance is no longer dominated by the scattering of the atoms in the junctions and the aperture.

Let us now consider the characteristic magnitude of the non-stationary current fluctuations. As seen from Eq. 4, one can discriminate between two terms: (i) “classical” backscattering related to the diagonal terms in the sum of Eq. 4 which is independent of the coordinates of the scatterers and thus not sensitive to relaxations; and (ii) the interference contribution due to the $N(N-1)$ non-diagonal terms proportional to cosines and depending on the positions of the atoms. For a given mode \mathbf{k} and for a given position \mathbf{r} in the detector plane the standard deviation of the interference term is $\sim \sqrt{N(N-1)} \sim N$. However, additional averaging over the $\sim N^{2/3}$ different modes and over the different positions of \mathbf{r} reduces the standard deviation to $N/(N^{2/3})^{1/2}(N^{2/3})^{1/2} = N^{1/3}$. Here positions separated by distances larger than $\sim 1/k$ are to be considered as independent, concerning the interference, giving in our units about $N^{2/3}$ independent positions. Therefore, the total standard deviation of the interference contribution due to a displacement of all scatterers is smaller than the average backscattered flow by about a factor of $N/N^{1/3} = N^{2/3}$. If one considers the current transport according to the concept of “quantum channels”, where in the weak scattering limit each elementary cell in the point contact orifice roughly corresponds to one channel, the standard deviation of the interference contribution is of the order of the contribution of one channel, in agreement with the picture of Universal Conductance Fluctuations (see e.g. Ref. 34). For a shift of a single scatterer (affecting N terms in the summation over i, j in Eq. 4) the effect is expected to be reduced by $N^{1/2}$ while for an uncorrelated jump of

M atoms the expected effect is $\sim M^{1/2}/N^{2/3}N^{1/2} \sim M^{1/2}N^{-7/6}$ (normalized with respect to the average backflow current). Thus a jump of about 15 atoms out of 500 should give a fluctuation of relative magnitude ~ 0.003 .

As seen, the order of magnitude of the experimental results is in agreement with this estimate. Some larger effects shown in Fig. 5 can be related to the fact that actually the jumps cannot be considered as incoherent shifts of M atoms; the coherency of the atomic motion can increase the observed effect. Qualitatively, the results show the decrease of the relative fluctuation with increasing N and with decreasing M . The magnitude of the fluctuations gives information about the size of the relaxing region and about the character of the motion.

The occurrence rate of the fluctuations is many orders of magnitude smaller than characteristic vibrational frequencies of the structure and thus we are obviously dealing with slowly relaxing degrees of freedom. However, for the simulated structures the rate is still much larger than a typical frequency for the telegraph noise observed in real experiments^{1,2}. The reason is again the instability of the structures studied with respect to crystallization which simply prevents long observation times which is in particular related to the small sizes of the systems and to the role of the periodic boundary conditions. In real systems relaxations would be slowed down due to strains exerted by the embedding material. In our point of view the simulations give a good model for the slowly relaxing multistable entities in real structures. The structures in real point contacts will be somewhere in between the amorphous and partially crystalline state. In this respect we would especially like to emphasize that the multistable defects were also demonstrated for the simulated crystalline defect structure of Fig. 5.

The simulated current fluctuations exhibit a rather complex time behaviour. The complex behaviour shown in Fig. 4 results from jumps connecting eight different configurations of nearly equal energy. Since the initial and final configurations are identical all jumps are reversible. Some jumps might trigger each other, others will occur randomly. E.g. after 42000 MDS a jump followed immediately by the return jumps occurs, 15000 MDS later the same jump is followed by two different jumps before returning to the start configuration. Actually the simulated picture resembles the one observed for real metallic contacts² at high enough temperatures referred to as “fluctuator melting”. We would like to emphasize that the slowing down of relaxations with temperature prevented us from studies of the extremely low temperatures where simpler two state telegraph signals are expected. We want to emphasize, however, that the temperatures of our simulations are still much below the glass-transition and melting temperatures. We see a similarity to real experiments² where “fluctuator melting” was observed at temperatures of about 100 K, i.e. much below the melting temperature of the metal. Our simulations show that typically the “fluotators” in-

volve large groups of atoms comprising up to 100 particles arranged mainly along some preferential direction. In Fig. 7 we show such a fluctuator identified by the of MD-simulations for the current noise shown in Fig. 4. The atoms contributing strongly to the relaxation are shown with their respective initial and final positions marked as full and shaded circles. The structure formed by the particles resembles a chain with side branches. Note that the displacement of the atoms from the initial minimum to the second one is nearly one-directional (along the chain). This fluctuator corresponds in Fig. 4 to the pronounced reversible relaxation after 42000 MDS with an effective mass $M_{\text{eff}} = 18m$ and a total displacement $\Delta R = 1.22\sigma$. Multistable configurations are more easily formed in the more complex Se structure. To some extent this hints towards a possible role of complex defects in the formation of fluctuators. In Fig. 8 we show the atoms, which strongly participate in the telegraph noise shown in Fig. 6 at $t < 250$ ps. The complexity of the relaxation is reflected by the fact that atoms of two regions of the system strongly participate in the jump. One of the structures of the relaxing entity is nearly one-dimensional and the atoms comprising this structure move cooperatively along this preferential direction. In particular, one can speculate on the apparent similarity between the helical structure in Se and the structure near the core of a screw dislocation. In this respect we would like to mention the experimental studies³⁵ where the observed $1/f$ noise was shown to originate from atomic motion near dislocation cores.

One notes that the picture of the current behaviour is more complex than simple fluctuations which average out over long enough time scales which are not accessible in MD-simulations. We observe a number of relaxations and related current fluctuations with different relaxation times. The time window of our simulation is too narrow to determine whether these fluctuations obey a $1/f$ law in the large ensemble or long time limits.

To conclude, in the framework of a simple model we have done a first simulation of multistable current noise in disordered contacts. The slowly relaxing modes responsible for the noise are visualized. The dependence of the noise magnitude on the size and structure of the modes was studied. In particular, the role of coherent atomic motion was emphasized. An important feature is a drastic change in the fluctuator dynamics (a transition to a complex multistable character of fluctuations) at temperatures of about a tenth of the melting temperature of the sample; this behaviour agrees with “fluctuators melting” reported for real metallic point contacts².

ACKNOWLEDGMENTS

We are indebted to H.R. Schober and V.L. Gurevich for reading the manuscript and for many valuable remarks and discussions. One of us (V.I.K.) acknowledges the

hospitality of the Institut für Festkörperforschung of the Forschungszentrum Jülich and the financial support by the German Ministry of Technology under the Russian-German scientific cooperation agreement. One of us (C.O.) gratefully acknowledges funding by the Deutsche Forschungsgemeinschaft through the Sonderforschungsbereich 408.

-
- * Permanent address: A.F.Ioffe Physico-Technical Institute, 194021 St.-Petersburg, Russia
 - ** Present address: Institut für Physikalische und Theoretische Chemie, Universität Bonn, D-53115 Bonn, and Institut für Algorithmen und Wissenschaftliches Rechnen, GMD – Forschungszentrum Informationstechnik, D-53754 Sankt Augustin, Germany.
 - ¹ C.T. Rogers and R.A. Buhrman, Phys. Rev. Lett. **53**, 1272 (1984).
 - ² K.S. Ralls and R.A. Buhrman, Phys. Rev. Lett. **60**, 2434 (1988).
 - ³ A.M. Kogan and K.E. Nagaev, Solid State Commun. **49**, 387 (1984).
 - ⁴ A. Ludviksson, R. Kree and A. Schmid, Phys. Rev. Lett. **52**, 950 (1984).
 - ⁵ V.I. Kozub, Sov. Phys. - JETP, **86**, 1303 (1984).
 - ⁶ V.I. Kozub, Sov. Phys. - Solid State, **26**, 1851 (1984).
 - ⁷ V.I. Kozub, Sov. Phys. - JETP, **60**, 818 (1984).
 - ⁸ Yu.M. Galperin, V.G. Karpov and V.I. Kozub, Adv. in Phys. **38**, 669 (1989).
 - ⁹ C.J. Muller, J.M. van Ruitenbeck, and L.J. de Jongh, Phys. Rev. Lett. **69**, 140 (1992).
 - ¹⁰ V.I. Kozub and A.M. Rudin, Phys. Rev. B **47**, 13737 (1993).
 - ¹¹ B.B. Laird and H.R. Schober, Phys. Rev. Lett. **66**, 636 (1991).
H.R. Schober and B.B. Laird, Phys. Rev. B **44**, 6746 (1991).
 - ¹² H.R. Schober, C. Oligschleger and B.B. Laird, J. Noncryst. Sol. **156-158**, 965 (1993).
H.R. Schober and C. Oligschleger, Phys. Rev. B **53**, 11469 (1996).
 - ¹³ J. Pelz and J. Clarke, Phys. Rev. B **36**, 4479 (1987).
 - ¹⁴ J.W. Martin, Phil. Mag. **24**, 555 (1971).
 - ¹⁵ Yu.M. Galperin and V.I. Kozub, Sov. Phys. - JETP, **73**, 179 (1991).
 - ¹⁶ C.W.J. Beenakker, H. van Houten, Quantum transport in semiconductor nanostructures in: Solid State Physics, **44**, Academic Press, 1991.
 - ¹⁷ L.I. Glazman et al., JETP Lett. **48**, 301 (1988).
 - ¹⁸ G. Kirczenow, Solid State Comm. **68**, 715 (1988).
 - ¹⁹ V.I. Kozub, J. Caro and P.A.M. Holweg, Phys. Rev. B **50**, 15126 (1994).
 - ²⁰ A. Grincwajg, G. Edwards and D.K. Ferry, Physica B **227**, 54 (1996).
 - ²¹ M. Born and E. Wolf, *Principles of optics: Electromagnetic Theory of Propagation and Diffraction of Light*, Pergamon

- Press, London, 1959, pp.374.
- ²² L.D.Landau, E.M.Lifshitz, *Quantum mechanics*, Pergamon, Oxford, 1972.
- ²³ C. Oligschleger and H.R. Schober, Physica A 201, 391-394 (1993)
- ²⁴ C. Oligschleger and H.R. Schober, Solid State Comm. Vol.93, No. 12, 1031-1035 (1995)
- ²⁵ W.G. Hoover, S.G. Gray, and K.W. Johnson, J. Chem. Phys. **55**, 1128 (1971).
- ²⁶ R. Fletcher, and C.M. Reeves, Comput. J. **7**, 149 (1964).
- ²⁷ C. Oligschleger and H.R. Schober, submitted
- ²⁸ H.R. Schober, C. Gaukel, and C. Oligschleger, Defect and Diffusion Forum **143-147**, 723 (1997).
- ²⁹ P. Ehrhart, K.H. Robrock, and H.R. Schober, in *Physics of Radiation effects in Crystals* (R.A. Jonson and A.N Orlov eds.), p.3, North Holland, Amsterdam: 1986.
- ³⁰ C. Oligschleger, R.O. Jones, S.M. Reimann, and H.R. Schober, Phys. Rev. B **53**, 6165 (1996)
- ³¹ T.N. Todorov and A.P. Sutton, Phys. Rev. Lett. **70**, 2138 (1993).
- ³² A.M. Bratkovsky, A.P. Sutton, and T.N. Todorov Phys. Rev. B **52**, 5036 (1995).
- ³³ T.N. Todorov and A.P. Sutton, Phys. Rev. B **54**, R14234 (1993).
- ³⁴ S. Feng, P.A. Lee, and A.D. Stone, Phys. Rev. Lett. **56**, 1960 (1986)
- ³⁵ E. Ochs, M.J.C. von Homberg, P.F.A. Alkemade, K. Armbruster, A. Seeger, H. Stoll, and A.H. Verbruggen, in *Noise in Physical Systems and 1/f Fluctuations: Proceedings of the 14th International Conference* (eds. C. Claeys and E. Simoen), p.415, World Scientific Pub. Co. (1997).

FIG. 1. Schematic plot of backscattered trajectories each involving one atom acting as scatterer of the incident electron wave. The incident wave is represented by its wave vector \mathbf{k} . Filled circles depict some of the atoms in the point contact. R_i and R_j denote the positions of the atoms and r the two-dimensional radius vector in the detector plane.

FIG. 2. Fluctuator behaviour of a configuration with $N = 500$ atoms. W_b is plotted against time in units of MDS. The reversible relaxation at $t \approx 25000\text{MDS}$ has an effective mass $M_{\text{eff}} = 16m$ and a total jump-length $\Delta R = 1.03\sigma$.

FIG. 3. Fluctuator behaviour of a configuration with $N = 1024$ atoms. W_b is plotted against time in units of MDS. The reversible relaxation at $t \approx 6000\text{MDS}$ has an effective mass $M_{\text{eff}} = 6m$ and a total jump-length $\Delta R = 0.44\sigma$.

FIG. 4. Fluctuator behaviour in a glass of 5488 soft spheres undergoing fifteen jumps between eight minima denoted by A,B,C,...,H. Different directions of detector planes are shown: (a) plane \perp x-axis and (b) plane \perp z-axis. Two direct reversible relaxations (with effective masses $M_{\text{eff}} = 16m$ and $M_{\text{eff}} = 18m$ and corresponding jump-lengths $\Delta R = 0.72\sigma$ and $\Delta R = 1.22\sigma$) can be observed. W_b is plotted against time in units of MDS.

FIG. 5. Fluctuator behaviour of a configuration with $N = 500$ atoms, which partially crystallized at a temperature $T = 0.05T_g$. The last three jumps with effective masses $M_{\text{eff}} = 74m, 72m, 74m$ have jump-lengths $\Delta R = 7.75\sigma, 6.83\sigma$ and 6.53σ , respectively. These relaxations are strongly correlated with $c_{RR'} = 0.958, 0.996$. W_b is plotted against time in units of MDS.

FIG. 6. Fluctuator behaviour of a configuration with $N = 750$ Se-atoms, at a temperature $T = 0.04T_g$. During the time-range $t = 15 - 260$ ps the glass switches between two configurations. The effective mass of the reversible jumps is $M_{\text{eff}} \approx 10$ and the jump-length $\Delta R \approx 0.5\text{\AA}$. The signal of the fluctuation is about 0.42% of the total contribution. W_b is plotted against time in units of ps.

FIG. 7. Reversible relaxation at $T = 0.1T_g$ observed in a glass with $N = 5488$ atoms. Full spheres depict the initial positions of the atoms, shaded spheres are the atomic positions after the relaxation. Shown are all atoms with a displacement more than 0.4 of the maximal contribution to this relaxation. The effective mass of this relaxation is $M_{\text{eff}} = 18m$ and the total jump-length is $\Delta R = 1.22\sigma$. The largest contribution of a single atom to this jump is $\Delta R_{\text{max}} = 0.29\sigma$. The backscattering contribution of this jump is shown in Fig. 4.

FIG. 8. Reversible relaxation at $T = 0.04T_g$ observed in a Se-glass with $N = 750$ atoms. Full spheres depict the initial positions of the atoms, shaded spheres are the atomic positions after the relaxation. Shown are all atoms with a displacement more than 0.2 of the maximal contribution to this relaxation. The maximal contribution to this relaxation is $\Delta R_{\text{max}} = 0.44\text{\AA}$. The backscattering contribution of this jump is shown in Fig. 6.

















